Cross-lingual document clustering is the task of automatically organizing a large collection of multi-lingual documents into a few clusters, depending on their content or topic. It is well known that language barrier and translation ambiguity are two challenging issues for cross-lingual document representation. To this end, we propose to represent cross-lingual documents through statistical word senses, which are automatically discovered from a parallel corpus through a novel cross-lingual word sense induction model and a sense clustering method. In particular, the former consists in a sense-based vector space model and the latter leverages on a sense-based latent
Dirichlet allocation. Evaluation on the benchmarking datasets shows that the proposed models outperform two state-of-the-art methods for cross-lingual document clustering.

**Keywords:** Word sense; cross-lingual document representation; cross-lingual document clustering.

1. **Introduction**

Economy globalization and internationalization of businesses urge organizations to handle an increasing number of documents written in different languages. As an important technology for cross-lingual information access, cross-lingual document clustering (CLDC) seeks to automatically organize a large collection of multi-lingual documents into a small number of clusters, each of which contains semantically similar cross-lingual documents.

Various document representation (DR) models have been proposed to deal with mono-lingual documents. The classic DR model is vector space model (VSM), which typically makes use of words as feature space. However, words are in fact not independent of each other. Two semantic word relations are worth mentioning, i.e. synonymy and polysemy. Synonymy indicates that different words can carry almost all identical or similar meaning, and polysemy implies that a single word can have two or more senses. To address such issues, previous researches attempted to represent documents through either explicit or latent semantic spaces.

In the cross-lingual case, DR models present two main issues: language barrier and translation ambiguity. As for the former, a term in one language and its counterparts in other languages should be viewed as a unique feature in cross-lingual DR. In some earlier systems, dictionaries were used to map cross-lingual terms. However, such systems all suffered from the latter issue, which implies that one term can be possibly translated into different terms in another language, especially when such terms entail common-sense knowledge. Two translation ambiguity scenarios are worth noting. In the first scenario, the term carries different meanings (namely, senses). For example, the word *arm* has two general meanings: (1) the part of body from shoulder to hand, and (2) a thing that is used for fighting. Accordingly, the word *arm* should be translated into 手臂 (shou3 bi4, arm) in a context relating to human body, but it should be translated as 装备 (zhuang1 bei4, arm) in a military context. The second scenario applies when we have to select one of the many possible translations to convey a specific meaning. For example, as a part of the human body, the word arm can be also translated into 脑神经 (ge1 bo2, arm), which is not quite the same as 手臂 (shou3 bi4, arm).

This is a common problem in natural language processing (NLP) research even in mono-lingual documents, e.g. when switching between different domains. In the context of CLDC, popular approaches consist in exploring word co-occurrence statistics within parallel/comparable corpora. Recent works improved clustering performance by aligning terms from different languages at topic-level. Nonetheless, cross-lingual topic alignment still remains an open challenge.
In this work, we treat translation ambiguity of terms, e.g. 手臂 (shou3 bi4, arm) and 装备 (zhuang1 bei4, arm), as polysemy and translation choices, e.g. 手臂 (shou3 bi4, arm) and 腕部 (ge1 bo2, arm), as synonyms. As synonymy and polysemy problems are closely related to word senses, we propose to represent document with cross-lingual statistical senses. Unlike previous approaches, which extract word senses from dictionaries, we propose to induce word senses statistically from corpora. To deal with cross-lingual cases, a novel cross-lingual word sense induction (WSI) model, referred to as CLHDP, is proposed to learn senses for each word (referred to as local word senses) respectively in parallel corpora. Thus, a sense clustering method is adopted to discover global word senses with semantic relatedness between senses of different words.

In this work, two cross-lingual DR models are proposed: a sense-based VSM and sense-based latent Dirichlet allocation (LDA) model. Two advantages of the proposed models are worth noting. Firstly, synonymy can be naturally addressed when word senses are involved. Words in one language that carry the same meaning can be organized by one word sense. In the cross-lingual case, words in cross languages can also be organized by one cross-lingual word sense. With synonymy addressed, cross-lingual documents can be more accurately represented. As a result, more accurate cross-lingual document similarity can be obtained and, hence, CLDC improves. Secondly, polysemy can also be well addressed as the translation ambiguity of polysemous words can be resolved within the cross-lingual contexts. Consequently, cross-lingual document similarity can be calculated more accurately when cross-lingual word disambiguation is achieved. By jointly addressing synonymy and polysemy, the proposed cross-lingual DR models work at a more semantic-level and, thus, are able to outperform bag-of-words models. Compared to topic-level DR models, moreover, the proposed models result to be more fine-grained and, hence, more accurate.

The structure of the paper is as follows: Section 2 introduces related work in the field of CLDC. Sections 3 and 4 illustrate in detail the proposed model. Section 5 presents evaluation and discussion. Section 6, finally, gives concluding remarks and future directions.

2. Related Work

2.1. DR models

This work is closely related to DR models. In traditional VSM, it is assumed that terms are independent from each other and, thus, any semantic relations between them are ignored. Previous works used concepts or word clusters as features or used similarities of words, but they still failed to handle the polysemy problem.

To address both of the synonymy and polysemy issues, some DR models are based on lexical ontologies such as WordNet or Wikipedia, to represent documents in a concept space. However, the lexical ontologies are difficult to construct and are
also hardly complete, moreover they tend to over-represent rare word senses, while missing corpus specific senses.

Representative extensions of the classic VSM are latent semantic analysis (LSA)\textsuperscript{20} and LDA.\textsuperscript{3} LSA seeks to decompose the term-document matrix by applying singular value decomposition, in which each feature is a linear combination of all words. However, LSA cannot solve the polysemy problem. LDA has successfully been used for the task of topic discovery\textsuperscript{3,21} but, according to Ref. 24, it may not perform well by itself in text mining task, especially in the case of tasks requiring fine granularity discrimination, e.g. document clustering. Most of these semantic models, moreover, are designed for mono-lingual document sets, and cannot be used in cross-lingual scenarios directly.

2.2. Cross-lingual document clustering

The main issue of CLDC is dealing with the cross-language barrier. The straight-forward solution is document translation. In TDT3, four systems attempted to use Machine Translation systems.\textsuperscript{22} Results show that using a machine translation tool leads to around 50\% performance loss, compared with mono-lingual topic tracking. This ascribed mainly to the poor accuracy of machine translation systems.

Dictionaries and corpora are two popular ways to get cross-language information. Some researches use dictionaries to translate documents.\textsuperscript{12} Others use dictionaries to translate features or keywords. Mathieu \textit{et al.} use bi-lingual dictionaries to translate named entities and keywords and modified the cosine similarity formula to calculate similarity between bi-lingual documents.\textsuperscript{25} Pouliquen \textit{et al.} rely on a multi-lingual thesaurus called Eurovoc to create cross-lingual article vectors.\textsuperscript{31} However, it is hard to select proper translation of ambiguous words in different contexts.

To solve such a problem, some researches leverage on word co-occurrence frequencies from corpora.\textsuperscript{12,25} However, they still need a dictionary but the human-defined lexical resources are difficult to construct and are also hardly complete. Wei \textit{et al.} use LSA to construct a multi-lingual semantic space onto which words and document in either language can be mapped and dimensions are reduced again according to documents to be clustered.\textsuperscript{41} Yogatama and Tanaka-Ishii use a propagation algorithm to merge multi-lingual spaces from comparable corpus and spectral method to cluster documents.\textsuperscript{45} Li and Shawe-Taylor use Kernel Canonical Correlation Analysis, a method that finds the maximally correlated projections of documents in two languages for cross-language Japanese-English patent retrieval and document classification.\textsuperscript{23}

Unlike document classification, document clustering usually lacks training data. Hence, semantic spaces are constructed from parallel/comparable corpora, and dimensions are selected on the basis of their importance in such corpora, which are usually different from the target multi-lingual documents. Mimno \textit{et al.} introduce a poly-lingual topic model that discovers topics aligned across multiple languages.\textsuperscript{27} However, topics generated from a parallel corpus may be not aligned well to the
topics discovered from the target document. Tang et al. use cross-lingual word similarity, but ignores the translation ambiguity problem.

In this work, we view language barrier and translation ambiguity as synonymy and polysemy problems and propose to use statistic word senses to represent documents in different languages. Our proposed model can concurrently deal with the problems of synonymy and polysemy and, hence, outperform the state-of-the-art CLDC methods.

2.3. WSI and disambiguation

Many approaches have been proposed to address the word sense disambiguation (WSD) task. The use of word senses has been proved to enhance performances on many NLP tasks. However, the use of word sense requires manually compiled large lexical resources such as WordNet.

In many other cases, word senses are learned from corpora in an unsupervised manner, known as WSI. Many WSI algorithms have been proposed in the literature. The Bayesian model proposed in Ref. uses an extended LDA model to induce word senses. It outperforms the state-of-the-art systems in SemEval-2007 evaluation by using a hierarchical Dirichlet process (HDP) to induce word senses. Unlike LDA, which requires a specified number of topics, HDP is able to infer such number automatically. Apidianaki uses a bi-lingual corpus and take translation equivalent clusters as word senses. It assumes that word instances with the equivalent translation carry the same meaning, which is not always true as instances of the same word with different meanings may be translated as the same word in another language.

WSI algorithms have already been integrated in information retrieval. However, to the best of our knowledge, the above-mentioned works only consider senses of query words, while in document clustering senses of every word in the documents should be identified.

In this paper, we propose to induce cross-lingual word senses from a parallel corpus by means of a novel Bayesian sense induction model, termed CLHDP, which is hereby also exploited for WSD.

3. CLDC System

3.1. An overview

Figure 1 presents the workflow of our sense-based CLDC system. Firstly, senses of individual words (referred to as local word senses) in each language are induced from the parallel corpus by means of a cross-lingual WSI (CL-WSI) algorithm. As a result, we obtain a set of local word senses, each of which is represented by distribution of cross-language words. Secondly, after grouping cross-language local word senses in one set, a clustering algorithm is used to partition such a set and, hence, to obtain a few word sense subsets, each of which contains some semantically similar
cross-language word senses. By using one sense for each subset to represent the different subsets, we obtain a few cross-lingual global word senses. Thirdly, cross-lingual documents are represented through such cross-lingual global word senses. Finally, the clustering algorithm is executed on the cross-lingual documents.

3.2. **Summary on novelty**

Two novel points in the CLDC system are worth noting.

1. We propose a cross-lingual WSI algorithm by adapting mono-lingual HDP to the cross-lingual scenario (CLHDP) and using a clustering method to discover semantic relatedness between senses of different words.
2. Cross-lingual DR models are proposed to represent cross-lingual documents with the cross-lingual word senses, which are learnt by means of the CLHDP algorithm on a parallel corpus.

In the next sections, we show how and why the proposed models are better than existing DR models and explain in detail modules of the systems.

4. **Theory and Algorithms**

4.1. **Definitions**

**Definition Local word sense**

A local word sense $s_w$ of word $w$ is statistically represented by a set of discrete distributions over context words — one for a specific language $l$, i.e.:

$$ s_w = \{ c^l_i : p(c^l_i|s_w) \} ; \quad i = 1, \ldots, N, $$

where $s_w$ denotes a local sense of word $w$, $c^l_i$ is a context word in language $l$, and $p(c^l_i|s_w)$ the probability distribution of $c^l_i$ under $s_w$.  

---

Fig. 1. Workflow of the CLDC system.
To obtain word senses, previous work relied on thesauri, which are time — and resource consuming to construct. In this work, instead, we use context words, as well as their probabilities to reflect word senses. To use word arm again as an example, the following two local word senses can be learnt from the corpus.

- arm#1={ limb: 0.159, forelimb: 0.069, sleeve: 0.019 }
- arm#2={ weapon: 0.116, war: 0.039, battle: 0.026 }

The example indicates that a local sense of the word arm involves specific context words and their probability values, which are estimated from the corpus through a WSI algorithm. Obviously, local word senses can address the polysemy issue.

**Definitions: Cross-lingual local word sense**

In the cross-lingual scenario, we extend the local word sense definition so that it involves multi-lingual context words, which are extracted from a parallel corpus, i.e.:

$$s_w = \left\{ \frac{c_{i}^{l_{k}}}{p(c_{i}^{l_{k}} | s_w)}, \quad i = 1, \ldots, N_{l_{k}}, \right\} \right\}$$

where $c_{i}^{l_{k}}$ is a context word in language $l_{k}$, and $p(c_{i}^{l_{k}} | s_w)$ the probability distribution of $c_{i}^{l_{k}}$ under $s_w$ within texts in language $l_{k}$. For the word arm in the English-Chinese scenario, for example, the following two cross-lingual local word senses are illustrative.

- arm#1={ limb: 0.159, forelimb: 0.069, sleeve: 0.019; 手臂: 0.137, 上肢: 0.079, 衣袖: 0.017 }
- arm#2={ weapon: 0.116, war: 0.039, battle: 0.026; 装备: 0.153, 武器: 0.027; 战争: 0.026 }

With an English-Chinese parallel corpus, the cross-lingual local word senses can be obtained through the CL-WSI algorithm. As seen in the above example, the cross-lingual local word senses can address the polysemy issue in cross-lingual scenarios. However, local word senses are induced for every word separately. It is very common that a large number of synonymous word senses exist. Hence, we further propose to learn global word senses, which represent the universally exclusive word senses.

**Definition: Cross-lingual global word sense**

A global word sense $g$ is a virtual word sense generalized from a group of synonymous local word senses, formalized as follows.

$$g = \{ s_{w}^{j} \}; \quad j = 1, \ldots, M,$$

where $s_{w}^{j}$ represents a local word sense. When the local word senses are induced from a cross-lingual scenario, the global word sense becomes cross-lingual naturally. In our CLDC system, the global word senses are discovered through a clustering algorithm.
that uses context words as features in calculating semantic similarity between local word senses. Again, we use the word arm as an example to illustrate the global word sense:

\[ g_{#1} = \{ \text{arm}_{#1}, \text{手脛}_{#1} \} = \{
  \{\text{limb}: 0.159, \text{forelimb}: 0.069, \text{sleeve}: 0.019; \text{手脛}: 0.137, \text{上脛}: 0.079, \text{衣袖}: 0.017\}, \\
  \{\text{arm}: 0.189, \text{forelimb}: 0.058, \text{sleeve}: 0.025; \text{胳膊}: 0.159, \text{上脛}: 0.089, \text{衣袖}: 0.014\}\}
\]

\[ g_{#2} = \{ \text{arm}_{#2}, \text{weapon}_{#1} \} = \{
  \{\text{weapon}: 0.116, \text{war}: 0.039, \text{battle}: 0.026; \text{武器}: 0.027, \text{战争}: 0.026\}, \\
  \{\text{arm}: 0.12, \text{battle}: 0.04, \text{war}: 0.016; \text{装备}: 0.133, \text{战士}: 0.028\}, \\
  \{\text{arm}: 0.14, \text{weapon}: 0.12, \text{war}: 0.016; \text{装备}: 0.133, \text{战争}: 0.035; \text{战士}: 0.028\}\}
\]

As shown in the above examples, the senses arm_{#1} and 手脛_{#1} are organized by the global word sense \( g_{#1} \) because the context distributions of arm_{#1} and 手脛_{#1} are similar. In this way, synonymous word senses in both languages can be organized with one global word sense. Synonymy is thus successfully addressed. In the following sections, we present how the cross-lingual word senses are learned from the parallel corpus.

### 4.2. Learning the cross-lingual word senses

Two steps are required in learning the cross-lingual word senses:

1. The local word senses are first induced from a parallel corpus;
2. The global word senses are generalized from the local word senses.

#### 4.2.1. Local WSI

The Bayesian model is adopted in order to achieve the task of local word sense learning. To be more specific, we extend HDP\(^{40}\) to the cross-lingual scenario, referred to as CLHDP. Theory of HDP is briefly introduced first.

**HDP for WSI**

HDP is proposed to perform text modeling. Yao and Van Durme (2011) employ HDP for WSI\(^{41}\). HDP should be performed on each word respectively, which means each word has its own HDP model. In this paper, we define a word on which the WSI algorithm is performed as a target word. We also define words in the context of a target word as context words of the target word.

HDP is a generative model, which can randomly generate observed data. For each context \( v_i \) of the target word \( w \), the sense \( s_{ij} \) for each word \( c_{ij} \) in \( v_i \) has a nonparametric prior \( G_i \) which is sampled from a base distribution \( G_w \). \( H_w \) is a Dirichlet distribution with hyperparameter \( \epsilon_w \). The context word distribution \( \eta_{sw} \) given a sense \( s_w \) is generated from \( H_w; \eta_{sw} \sim H_w \). The generative process of a target
word \( w \) is given as follows:

1. Choose \( G_w \sim DP(\gamma_w, H_w) \).
2. For each context window \( v_i \) of word \( w \):
   a. choose \( G_i \sim DP(\rho_w, G_w) \).
   b. for each context word \( c_{ij} \) of target word \( w \):
      i. choose \( s_{ij} \sim G_i \).
      ii. choose \( c_{ij} \sim \text{Mult}(\eta_{s_{ij}}) \).

Hyperparameters \( \gamma_w \) and \( \rho_w \) are the concentration parameters for DP, controlling the variability of the distributions of \( G_w \) and \( G_i \), respectively. HDP is illustrated in Fig. 2, where the shaded circle represents the observed variable, context word \( c_{ij} \). HDP can be generated by the stick-breaking process and the Chinese restaurant process.\(^{40}\)

### CLHDP model

CLHDP models word senses through cross-lingual context tuples. Each tuple is a set of contexts that are equivalent to each other but written in different languages. Two assumptions are made in CLHDP. Firstly, contexts in a tuple share the same tuple-specific distribution over senses. Secondly, each sense consists of a set of discrete distributions over context words — one for each language \( l = 1, \ldots, L \). In other words, rather than using a \( \eta_s \) for each sense \( s \), as in HDP, there are \( L \) language-specific senses-context word distributions \( \eta^l_s, \ldots, \eta^L_s \), each of which is drawn from a language-specific symmetric Dirichlet \( H^l_w \) with concentration parameter \( \lambda^l_w \). CLHDP is illustrated in Fig. 3.

As shown in Fig. 3, the generative process of a target word \( w \) is given as follows:

1. Choose \( G_w \sim DP(\gamma_w, H) \).
2. For each context window \( v_i \) of \( w \):
   a. choose \( G_i \sim DP(\rho_w, G_w) \).
   b. for each context word \( c^l_{ij} \) in language \( l \) of target word \( w \):
      i. choose \( s^l_{ij} \sim G_i \).
      ii. choose \( c^l_{ij} \sim \text{Mult}(\eta^l_{s_{ij}}) \).

---

**Fig. 2.** Illustration of the CLHDP model.

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Hyperparameters $r_w$ and $\rho_w$ are the concentration parameters of the DP, controlling the variability of the distributions $G_w$ and $G_{ui}$.

**Inference for CLHDP model**

Teh et al. use Collapse Gibbs Sampling to find latent variables in HDP. Gibbs Sampling initializes all hidden variable randomly.\textsuperscript{40} For each iteration, hidden variables are sequentially sampled from the distribution conditioned on all other variables. Three sampling schemes can be used in HDP: posterior sampling in Chinese restaurant franchise, posterior sampling with an augmented representation and posterior sampling by direct assignment.

For CLHDP, we use the direct assignment scheme because it is easy to implement. There are three steps in sampling scheme:

1. Given $s = \{s_{ij}\}$ and $m = \{m_{kj}\}$ in Chinese restaurant process, samples $\{G_v\}$ and $G_w$, where $m_{kj}$ represents the number of tables in restaurant $k$ serving dish $j$. The process is similar as described in Ref.\textsuperscript{40}.

The prior distribution $G_w$ for each target word is a Dirichlet Process with concentration parameter $\gamma_w$ and base probability $H_w$. It can be expressed using a stick-breaking representation,

$$G_w = \sum_{s_w=1}^{\infty} \pi_{s_w}^w \delta(\eta_{s_w}^1, \ldots, \eta_{s_w}^L),$$

where $\eta_{s_w}^1, \ldots, \eta_{s_w}^L$ are generated from $H_w^1, \ldots, H_w^L$ respectively and are given in this step, $\delta(\eta_{s_w}^1, \ldots, \eta_{s_w}^L)$ is a probability measure concentrated at $\eta_{s_w}^1, \ldots, \eta_{s_w}^L$. $\{\pi_{s_w}^w\}$ are mixtures over senses. They are sampled from a stick-breaking construction. In the sampling process, suppose that we have seen $S_w$ senses for the target word $w$. The context word distributions $\{\eta_{s_w}^1\}$ are generated and assigned to the context words in the corpus after some sampling iterations. $G_w$ can be expressed as

$$G_w = \Sigma_{s_w} \pi_{s_w}^w \delta(\eta_{s_w}^1, \ldots, \eta_{s_w}^L) + \pi_{w}^u G_{wu},$$

Fig. 3. Illustration of the CLHDP model.
where \( G_w^u \) is distributed as Dirichlet Process \( DP(\gamma_w, H_w) \). Thus, \( G_w \) is dependent on
\( \pi_w = \{ \pi_w^s \} \) and the sampling equation for \( \pi_w \) is as follows:

\[
(\pi_w^1, \ldots, \pi_w^s, \ldots, \pi_w^u) \mid \{\eta_{sw}\}, s \sim \text{Dir}(m_1, \ldots, m_s, \gamma_w),
\]

where \( m_j \) represents the number of tables in all restaurants serving dish \( j \).

(2) Given \( \{G_v\}, G_w \), sample \( s = \{s_{ij}\} \). The conditional probability for sampling the sense \( s_{ij} \) of context word \( c_{ij} = c \) in context window \( v_i \) in language \( l \) can be estimated as:

\[
P(s_{ij} = s_w \mid s_{-ij}, c_i) = \begin{cases}
(n_{-ij,s_w} + \rho_w \pi_w^s) \frac{n_{-ij,s_w}^c + \lambda_w^l}{n_{-ij,s_w} + V_{l,w} \lambda_w^l} & \text{if } s \text{ is previously used,} \\
\rho_w \pi_w^s \frac{n_{-ij,s_w}^c + \lambda_w^l}{n_{-ij,s_w} + V_{l,w} \lambda_w^l} & \text{if } s \text{ is new,}
\end{cases}
\]

where \( n_{-ij,s_w}^c \) is a count of how many context words \( = c \) are assigned sense \( s_w \), excluding the \( j \)th context word in language \( l \) and \( V_{l,w} \) is the number of context words in language \( l \). \( n_{-ij,s_w} \) is the total number of context words in language \( l \) that are assigned sense \( s_w \), excluding the \( j \)th context word in language \( l \), \( n_{-ij,s_w}^c \) is total number of context words in language \( l \) in \( v_i \) that are assigned sense \( s_w \) excluding the \( j \)th context word in language \( l \).

(3) Given \( G_w, s = \{s_{ij}\} \), sample \( m = \{m_{kj}\} \). The conditional probability for sampling \( m = \{m_{kj}\} \) can be estimated as:

\[
p(m_{kj} = m \mid s, m_{-kj}, \pi_w) = \frac{\Gamma(\rho_w \pi_w^s)}{\Gamma(\rho_w \pi_w^s + n_{k,j})} s(n_{k,j}, m)(\rho_w \pi_w^s)^m,
\]

where \( n_{k,j} \) represents the number of customers in restaurant \( k \) serving dish \( j \); \( s(n_{k,j}, m) \) are unsigned Stirling numbers of the first kind.

Thus the context word distribution \( \eta_{sw}^l \) can be calculated as

\[
\eta_{sw}^l(c) = \frac{n_{s_w,l}^c + \lambda_w^l}{n_{s_w,l} + V_{w,l} \lambda_w^l}
\]

where \( n_{s_w,l}^c \) is a count of how many context words \( = c \) are assigned sense \( s \), in language \( l \) and \( V_{w,l} \) is the number of context words in language \( l \), \( n_{s_w,l} \) is the total number of words in language \( l \) that are assigned sense \( s_w \).

In this work, we use sentences as context windows and extract cross-lingual context in a parallel corpus. For example, when a word is found in one sentence, we put the sentence and its corresponding sentence in the parallel corpus in a tuple.

**4.2.2. Global word sense generalization**

We view word sense generalization as a clustering task. The goal is to organize semantically similar word senses with one virtual word sense, which is globally unique.
In this work, probability distribution of context words is considered as a set of features and clustering algorithms are applied to merge equivalent senses. For a cross-lingual word sense, we simply combine context words in all languages and their distributions in one vector.

Two methods are adopted to cluster the local word senses:

1. **Bisecting K-Means** is an extension of K-means, which is proven better than standard K-Means and hierarchical agglomerative clustering. It begins with a large cluster consisting of every element to be clustered and iteratively picks the largest cluster in the set and splits it into two.

2. **Graph-based Clustering** is a clustering method based on graph-partition. It first models the objects using a nearest-neighbor graph and then splits the graph into k-clusters using a min-cut graph-partitioning algorithm.

### 4.3. Sense-based DR

#### 4.3.1. Cross-lingual WSD

In this work, the CLHDP algorithm is also used for WSD. Given $D = \{d_j; j = 1, \ldots, N\}$ representing a document set containing $N$ documents and $M$ words, the context set for each word is extracted and sense distribution in each context can be estimated by CLHDP model.

Given the word $w$ in language $l$, the sense-context word distribution $\eta_{sw}$ for word $w$ estimated in parallel corpus, context sets $\{\hat{v}_i; i = 1, \ldots, \hat{V}_w\}$ in $D$, the inference process is similar as Sec. 4.2.1. The only modification is that in the second step, the conditional probability for sampling the sense $s_{ij}$ of context word $c_{ij} = c$ in context window $\hat{v}_i$ in language $l$ can be estimated as:

$$ P(s_{ij} = s_w; s_{-ij}, c_i) = (\hat{n}_{-ij,s_w} + \hat{\rho}_w \hat{\pi}_w)\eta_{sw}(c_{ij}), $$

where $\hat{n}_{-ij,s_w}$, $\hat{\rho}_w$, $\hat{\pi}_w$ represent CLHDP parameters in context sets $\{\hat{v}_i; i = 1, \ldots, \hat{V}_w\}$.

After sampling, the sense distribution $\theta_\hat{v}$ for each context window $\hat{v}_i$ in context set $\{\hat{v}_i; i = 1, \ldots, \hat{V}_w\}$ for the target word $w$ can be estimated as follows:

$$ \theta_\hat{v}(s_w) = \frac{\hat{n}^{\hat{v}}_{s_w} + \hat{\rho}_w \hat{\pi}_w}{\hat{n}^{\hat{v}} + \hat{\rho}_w \sum s^\hat{v}_w \hat{\pi}_w}, $$

where $\hat{n}^{\hat{v}}_{s_w}$ is a count of how many sense $s_w$ in context window $\hat{v}$ and $\hat{n}^{\hat{v}}$ is the total number of words in context window $\hat{v}$.

With $\theta_\hat{v}(s_w)$, we simply take the mode sense in the distribution as the sense of the target word.

For example, three sentences are given below.

- $S_1$: That man with one arm lost his other limb in an airplane crash.
- $S_2$: The nation must arm its soldiers for battle.
After stop word removal and word lemmatization, the three sentences become:

- \( S_1: \text{man arm lost limb airplane crash} \)
- \( S_2: \text{nation arm soldier battle} \)
- \( S_3: \text{国家必须为了战争武装它的士兵。} \)

The probability of word sense \( \text{arm}#1 \) in sentence \( S_1 \) is 0.998005. For sentence \( S_2 \), the probability of word sense \( \text{arm}#2 \) is 0.944096.

In this work, we simply take the sense with the highest probability as the sense of the target word and use the senses to represent document. So the sense of arm in \( S_1 \) is \( g#1 \) because the probability of \( \text{arm}#1 \) is higher and \( \text{arm}#1 \) belongs to \( g#1 \). Similarly, the sense of arm in \( S_2 \) is \( g#2 \).

For sentence \( S_3 \), the sense of 装(wu3 qi4, arm) is also \( g#2 \). In this way, instances of the same word with different meanings are identified as different senses and different words with same meaning are identified as the same sense. Accordingly, translation ambiguity and language barrier issues are both addressed.

After WSD, we start from the two most popular DR models, i.e. VSM and LDA, and propose sense-based versions of them.

### 4.3.2. Sense-based VSM

The traditional VSM model uses discriminative words to represent a document. Document \( d_i \) in document set \( D \) is represented as \( d_i = \{ w_{ij} : r_{ij} \}_{j=1,...,M^{d_i}} \) in VSM, where \( r_{ij} \) represents the weight of a feature word \( w_{ij} \) in \( d_i \). \( M^{d_i} \) is the number of feature words in \( d_i \).

Differently, sense-based VSM (sVSM) uses global senses as features. With WSD, every word first in the document is assigned a unique global sense. Then, the weight of a global sense is calculated in a similar manner using TF-IDF formula. Finally, the sense vector is produced for each document. For example, \( d_i \) can be represented as \( d_i = \{ g_{ij} : \hat{r}_{ij} \}_{j=1,...,M^{d_i}} \) in sVSM, where \( \hat{r}_{ij} \) represents the weight of sense \( g_{ij} \) in \( d_i \). We use cosine similarity to calculate similarities between two sense vectors.

### 4.3.3. Sense-based LDA

We replace word surfaces with word senses so that the classic LDA model is extended to sense-based LDA (sLDA) model. The WSD algorithm is again used to assign a unique global sense to a specific surface word. Then, sLDA generates a distribution of topics \( \theta_{d_i} \) for each document \( d_i \) in the document set. For a word \( w_j \) in the document, the sense \( s_{ij} \) is drawn from the topic and topic-sense distribution \( \phi \) containing \( T \) multinomial distributions over all possible senses in the corpus drawn from a symmetric Dirichlet distribution \( \text{Dir}(\beta) \).
As shown in Fig. 4, the formal procedure of generative process in sLDA is given as follows:

1. For each topic $z$:
   (a) choose $\hat{\phi}_z \sim \text{Dir}(\hat{\beta})$.

2. For each document $d_i$:
   (a) choose $\hat{\theta}_{d_i} \sim \text{Dir}(\hat{\alpha})$.
   (b) for each word $w_j$ in document $d_i$:
      (i) choose topic $z_{ij} \sim \text{Mult}(\hat{\theta}_{d_i})$.
      (ii) choose sense $g_{ij} \sim \text{Mult}(\hat{\phi}_{z_{ij}})$.

In sLDA, Gibbs sampling is used for parameter estimation and inference. Compared with LDA, we replace the surface words with the induced word senses. Therefore, the topic inference is similar to the classic LDA, where the condition probability $P(z_{ij} = z | z_{-ij}, s)$ is evaluated by

$$P(z_{ij} = z | z_{-ij}, s) \propto \frac{n_{d_i}^{z_{ij}} + \alpha}{n_{-ij}^{z_{ij}} + Z\alpha} \times \frac{n_{ij,z}^{g} + \beta}{n_{-ij,z}^{g} + G\beta}. \quad (12)$$

In Eq. (12), $n_{d_i}^{z_{ij}}$ is the number of words that are assigned topic $z$ in document $d_i$; $n_{-ij}^{z_{ij}}$ is the total number of words in document $d_i$; $n_{ij,z}^{g}$ is the number of senses with sense $g$ that are assigned topic $z$; $n_{-ij,z}$ is the total number of words assigned topic $z$; $G$ is the number of senses for the dataset. $-ij$ in all the above variables refers to excluding the count for the sense of the $j$th word. Further details are similar to the classic LDA.

### 4.4. Cross-lingual document clustering

Document clustering becomes naturally feasible when the documents are represented by cross-lingual word senses. As the clustering algorithm is not the focus of this work, we simply adopt Bisecting K-Means to cluster document for sVSM. For sLDA, each topic in the test dataset is considered a cluster. After the parameters are estimated, documents are clustered into topics with the highest probabilities.
5. Evaluation

5.1. Setup

Development dataset
We randomly extract 1M parallel sentence pairs from LDC corpora (i.e. LDC2004E12, LDC2004T08, LDC2005T10, LDC2002E14, LDC2002E18 LDC2005T06, LDC2003E07 and LDC2004T07) as our development data to get word senses.

Test dataset
Four datasets are used in this paper.

(1) TDT4 datasets: Following Kong and Graff,\textsuperscript{19} we use two datasets which are extracted from TDT4 evaluation dataset.
(2) CLTC datasets: Two datasets are extracted from the CLTC.\textsuperscript{39}

Table 1 presents statistics of the four datasets.

In our experiments, we only extract nouns and verbs to induce word senses because words of other types make little contribution in document clustering. We use TreeTagger\textsuperscript{33} to do lemmatization and POS tagging for English word, and use ICTCLAS\textsuperscript{a} to segment Chinese words and assign POS tags to these words. Word information of the four test datasets is presented in Table 2.

Evaluation metrics
We adopt the evaluation metrics proposed by Steinbach \textit{et al.}\textsuperscript{36} The evaluation metrics are defined as the maximum score for each cluster. Let $A_i$ correspond to the set of articles in a human-annotated cluster $c_i$. Let $A_j$ correspond to the set of articles

\begin{table}[h]
\centering
\caption{Statistics of topic and story in the four datasets. In each cell, number of topics is on the left and number of stories on the right.}
\begin{tabular}{ lccccc }
\hline
\hline
English & 38/1270 & 33/617 & 20/200 & 20/600 \\
Chinese & 37/657 & 32/560 & 20/200 & 20/600 \\
Common & 40/1927 & 37/1177 & 20/200 & 20/1200 \\
\hline
\end{tabular}
\end{table}

\begin{table}[h]
\centering
\caption{Word statistics in the four datasets.}
\begin{tabular}{ lcccc }
\hline
\hline
English & 2414 & 1887 & 1651 & 1862 \\
Chinese & 5457 & 3548 & 1437 & 2255 \\
Common & 7871 & 5435 & 3088 & 4117 \\
\hline
\end{tabular}
\end{table}

\textsuperscript{a}http://www.ictclas.org/ictclas\_introduction.html.
in a system-generated cluster $c_j$. We consider each topic in the dataset as a cluster. The score for each cluster is based on the pairwised evaluation as follows:

$$p_{i,j} = \frac{|A_i \cap A_j|}{|A_i|}, \quad p_i = \max_j \{p_{i,j}\},$$

$$r_{i,j} = \frac{|A_i \cap A_j|}{|A_j|}, \quad r_i = \max_j \{r_{i,j}\},$$

$$f_{i,j} = \frac{2 \cdot p_{i,j} \cdot r_{i,j}}{p_{i,j} + r_{i,j}}, \quad f_i = \max_j \{f_{i,j}\},$$

where $p_{i,j}$, $r_{i,j}$ and $f_{i,j}$ represent precision, recall and F-measure for the pair of clusters $c_i$ and $c_j$, respectively. The general F-measure of a system is the micro-average of all the F-measures ($\{f_i\}$) for the system-generated clusters.

**System parameters**

The proposed approach involves great flexibility in modeling empirical data. This, however, entails that several parameters must be instantiated. More precisely, our model is regulated by the following four kinds of parameters:

1. WSI parameters: We set $\Gamma(1, 0.1)$, $\Gamma(0.01, 0.028)$ and $\lambda = 0.1$ for every word and both languages.
2. sVSM parameters: We set number of clusters as number of topics in each dataset.
3. sLDA parameters: We set $\alpha = 50/\#\text{topic}$, $\beta = 0.1$ which are usually used in LDA. The topic number is also set as cluster number in each dataset. In all experiments, we let the Gibbs sampler burn in for 2000 iterations and subsequently take samples 20 iterations apart for another 200 iterations.
4. Number of global senses: We choose to conduct experiments to observe how they influence the document clustering performance.

**5.2. Experiment 1: Different word sense clustering methods**

In this experiment, we aim to study how different word sense clustering (WSC) methods influence the system performance. We implement two systems of different WSC methods.

1. **Bisecting K-Means with sVSM (BK-sVSM):** The system uses Bisecting K-means to cluster local word sense. sVSM is used to represent documents. Cosine similarity measure is used to calculate document similarity and Bisecting K-means is used to cluster documents.
2. **Graph-based Clustering with sVSM (GC-sVSM):** The system uses Graph-based clustering method to cluster local word sense. Other setups are the same as BK-sVSM.
We incrementally increase sense number $|G|$ from 100 to 4000 and evaluate both systems with the four datasets separately. Experimental results are presented in Figs. 5–8. The best F-measure values ($f_1$) at the corresponding global word sense number (i.e. $f_1@Number \#$) of the two systems are listed in Table 3. The average efficiency of the two systems are listed in Table 4.

Fig. 5. Results of the systems with different sense numbers in CLTC1 test dataset.

Fig. 6. Results of the systems with different sense numbers in CLTC2 test dataset.

Fig. 7. Results of the systems with different sense numbers in TDT41 test dataset.
Discussion on influence of the global sense number

We compared the performance of different sense numbers and found that using low and high sense number can cause a drop on F-measure. This is due to the fact that, when the sense number is set to a low number, many local word senses that are not similar are clustered together resulting in low performance. When the sense number is set to a high number, similar local word senses are not clustered together. Thus, words with the same meaning in different languages may not be connected. This will largely affect the accuracy of similarity between documents in different languages. In that case, performance is reduced. After comparing different datasets, we can claim that datasets with larger word number have larger optimal global word sense number. For example, in system BK-sVSM, in CLTC1 dataset with 3088 words, the best F-measure achieves when the global word sense number is set as 700 while in TDT41 dataset with 7871 words, the optimal global word sense number is 1800. This is coherent with the fact that dataset with more words usually contains more senses.
Discussions on influence of the sense clustering method
As we can see from Figs. 5–8, BK-sVSM system outperforms GC-sVSM when the
sense number \(|G|\) increases from 100 to 3500 in most cases. This happens because the
graph-based clustering method produces unbalanced clusters, while bisecting
K-Means is more balanced in which it favors global property rather than the nearest
neighbor. For this reason, we use Bisecting K-Means in WSC in the later experiments.

From Table 4 we can see GC-sVSM is much faster than BK-sVSM. This is be-
cause given \(n\) as the number of objects to be clustered, the time complexity of
Bisecting K-Means is \(O(\text{NNZ} \times \log(k))\) where \(\text{NNZ}\) represent the number of nonzeros
in the input matrix while the time complexity of Graph-based Clustering is
\(O(n^2 + n \times \text{NNbrs} \times \log(k))\) where \(\text{NNbrs}\) represents the number of neighbors in the
nearest-neighbor graph. The number of target words is much smaller than the
number of context words. So \(\text{NNZ}\) is much larger than \(n^2\) and the time complexity of
Bisecting K-Means is larger than the time complexity of Graph-based Clustering.

5.3. Experiment 2: Different sense-based DR models
In this experiment, we aim to study how different DR models influence system
performance. Besides BK-sVSM, we also implement a system using sLDA to rep-resent
documents.

(1) BK-sLDA: The system uses sLDA to represent documents.

Experimental results on four datasets in two language cases are given in
Figs. 9–12. The best F-measure (f1) at the corresponding global word sense number
(i.e. f1@topic #) of the two systems are listed in Table 5.

Discussion
We compared the performance of different DR models based on sense and found that
sVSM outperforms sLDA in all datasets. This is because fine granularity discrimi-
nation of feature space is important in document clustering task, while topic inferred
from LDA may not resolve this issue very well. This is consistent with Ref. 24.

Fig. 9. Results of the systems with different sense numbers in CLTC1 test dataset.
Table 5. The highest F-measure values of CLDC with different sense-based DR models in four test sets.

<table>
<thead>
<tr>
<th>System</th>
<th>CLTC1</th>
<th>CLTC2</th>
<th>TDT41</th>
<th>TDT42</th>
</tr>
</thead>
<tbody>
<tr>
<td>BK-SVSM</td>
<td>0.926@700</td>
<td>0.904@1300</td>
<td>0.809@1800</td>
<td>0.791@1500</td>
</tr>
<tr>
<td>GC-SVSM</td>
<td>0.774@2000</td>
<td>0.847@2900</td>
<td>0.795@3100</td>
<td>0.780@1900</td>
</tr>
</tbody>
</table>
5.4. Experiment 3: Different document representation models

In this experiment, we intend to compare our model with state-of-the-art DR models in CLDC. Besides BK-sVSM, the following two models are implemented.

1. **CL-GVSM**: The model proposed by Tang et al. improves the similarity calculation by cross-lingual word similarity from a parallel corpus.\(^{39}\)

2. **PLTM**: The model proposed by Mimno et al. to get cross-lingual topic information.\(^{27}\) In this paper, we apply the model on the parallel corpus to train cross-lingual topic and infer the topic distribution on the test dataset. The topic number is set to 1000. Bisecting K-means is used to cluster documents with the topic distribution as features.

Experiment results on four datasets in two language cases are given in Table 6.

**Discussion**

As shown in Table 6, BK-sVSM outperforms GVSM in all datasets. GVSM is a DR model that considers word similarity. However, it only considers relationships between words and ignores differences of one word in different contexts, which instead our proposed BK-sVSM considers both.

Table 6 also shows that BK-sVSM outperforms PLTM in all datasets. This indicates BK-sVSM outperforms PLTM in document clustering task. We find that PLTM yields the lowest performance in most cases. The reason for the significant performance drop is that, when using a parallel corpus to train the PLTM model, the topics may not be well covered in the test dataset and noise redundant topics (produced by the training corpus) may affect the performance.

**Performance issue**

Inducing word senses from the development data and clustering the word senses require higher computational effort. Indeed, the most time-consuming phase of our proposed model is the construction of word senses, which requires one CLHDP model for each word and a clustering method on those topics, referred to as local word senses in this paper. While word senses can be pre-computed or cached, word disambiguation of the test datasets still requires to be computed in real time. However, it can take advantage of parallel computing in which the disambiguation of each word is independent.

<table>
<thead>
<tr>
<th>System</th>
<th>CLTC1</th>
<th>CLTC2</th>
<th>TDT41</th>
<th>TDT42</th>
</tr>
</thead>
<tbody>
<tr>
<td>BK-SVSM</td>
<td>0.926</td>
<td>0.904</td>
<td>0.809</td>
<td>0.791</td>
</tr>
<tr>
<td>GVSM</td>
<td>0.900</td>
<td>0.898</td>
<td>0.762</td>
<td>0.748</td>
</tr>
<tr>
<td>PLTM</td>
<td>0.768</td>
<td>0.776</td>
<td>0.493</td>
<td>0.482</td>
</tr>
</tbody>
</table>
6. Conclusion

Previous researches show the importance of addressing language barrier and translation ambiguity in CLDC. In this paper, these two issues are viewed as general synonymy and polysemy problems and a DR based on cross-lingual statistical word senses is proposed.

The proposed method, in particular, aims to address the synonymy and polysemy issues in DR in two ways: (1) words containing the same meaning in different languages can be identified as the same word senses (in that case, language barrier can be crossed); (2) Instances of the same word with different meanings are identified as the different word senses (in that case, translation ambiguity can be addressed). Experiments on four datasets of two language cases show that our proposed model outperforms two state-of-the-art models in CLDC.

In the future, we plan to evaluate the performance of the proposed method with datasets of smaller samples. As the proposed method represents document in a word sense space, in fact, we can utilize it to handle sparse data problem with datasets of smaller samples, e.g. SMS messages and tweets.

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References


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